

# 1016-351-01 Probability

## Problem Set 3

Assigned 2011 December 13  
Due 2012 January 10

Show your work on all problems! If you use a computer to assist with numerical computations, turn in your source code as well.

- 1 Devore Chapter 3, Problem 12
- 2 Devore Chapter 3, Problem 18
- 3 Devore Chapter 3, Problem 32
- 4 Devore Chapter 3, Problem 46
- 5 Computational Exercise (Extra Credit)

Consider the pmf from Chapter 3, Problem 12 for the number  $Y$  of ticketed passengers, out of 55, who show up for a flight.

$y$	45	46	47	48	49	50	51	52	53	54	55
$p_Y(y)$	.05	.10	.12	.14	.25	.17	.06	.05	.03	.02	.01

A reasonable supposition is that each passenger has an independent probability  $p$  of showing up, in which case the number of passengers showing up would be a binomial random variable  $X \sim \text{Bin}(55, p)$ . (Obviously, that's not exactly the situation described in the problem, since  $p_Y(y) = 0$  for  $y < 45$ , which won't be the case for  $p_X(x)$ .)

- a. Calculate  $E(Y)$  from the pmf.
- b. Find the value of  $p$  such that  $E(X) = E(Y)$ .
- c. Using this value for  $p$ , make a table of the values of  $p_X(x)$  for  $45 \leq x \leq 55$  to two decimal places (*not* two significant figures), and compare the results to the table above.
- d. Calculate  $F_X(44) = P(X < 45)$  to two decimal places. (Note that  $F_Y(44) = P(Y < 45) = 0$ .)