

# 3-D GRMHD Simulations of Accreting Binary Black Holes

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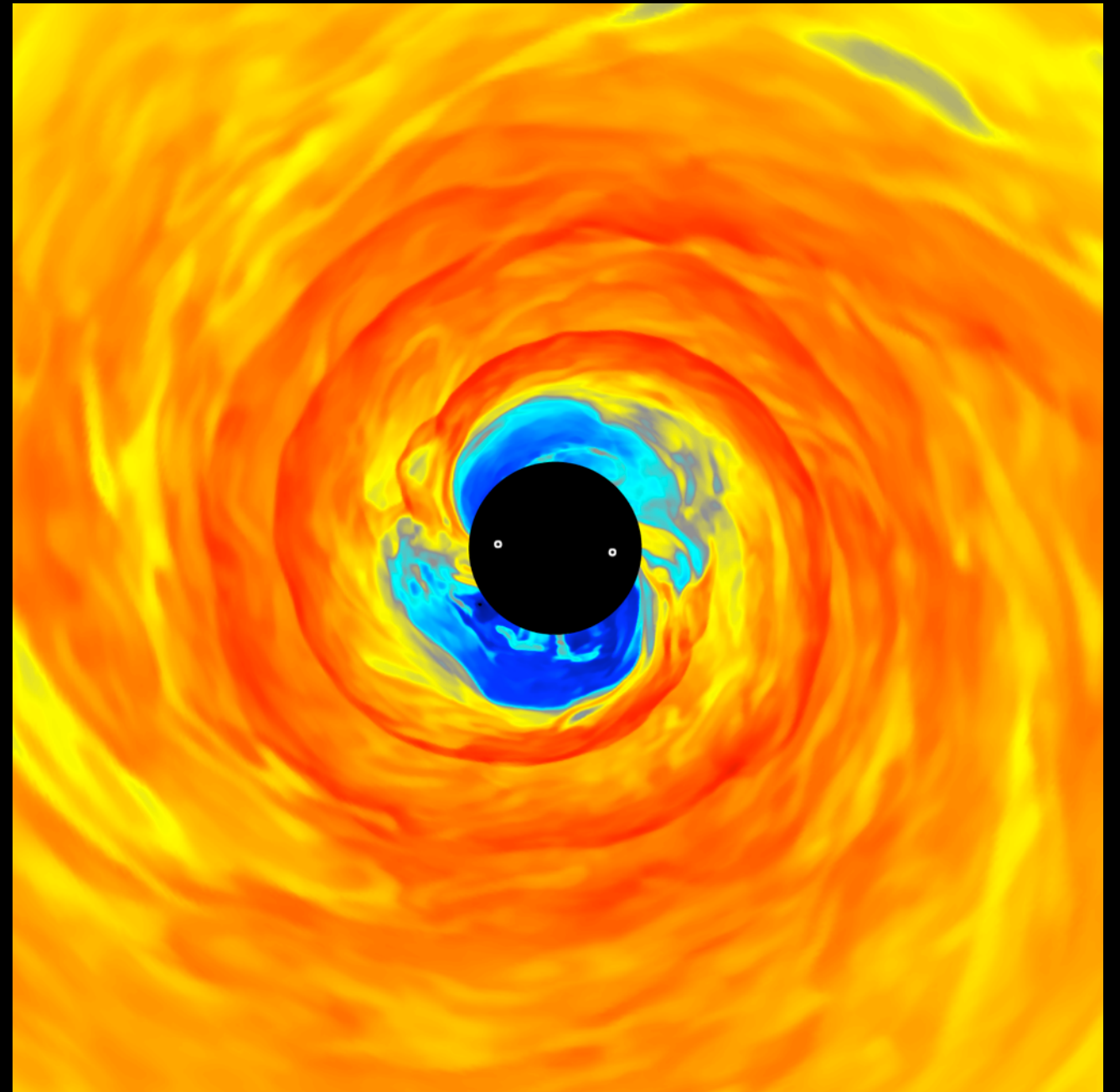
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Based on:

- Noble++2012
- Zilhao & Noble 2014
- Zilhao++2015 (in press, PRD)
- Noble++in-prep



**Thanks to NSF PRAC OCI-0725070 & NSF CDI AST-1028087**

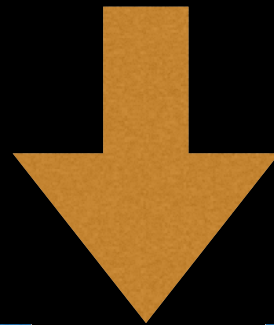
“Black Holes in Dense Star Clusters” — Aspen — Winter — 2015

# Motivation

**Rare  
Events**

+

**Degeneracy  
of  
Interpretations**



**More Data**  
(Pan-STARRS,  
LSST, ZST, PST...)

+

**Better Models**  
+MHD  
+3-d  
+GR  
+Radiation Cooling  
+Radiation Feedback

# Motivation

## Better Models

+MHD

+3-d

+GR

+Radiation Cooling

+Radiation Feedback

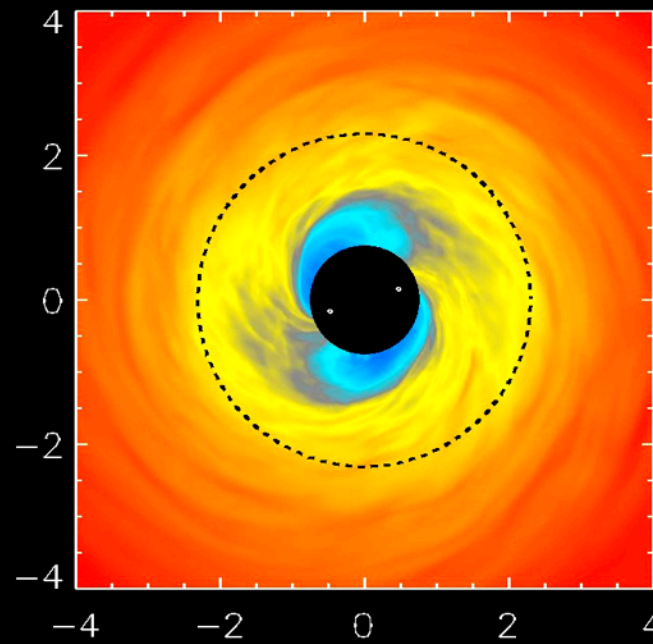
- MHD turbulence = Ang. Mom. transporter;
- Field dissipation and growth cannot be modeled w/ 2-d hydro;
- Vertical, 3-d structure can only include dynamics of buoyancy;
- Cowling's Thm: no sustained turbulence in 2-d;
- Post-Newtonian (PN) accuracy required for binary separations below  $\sim 100M$ ;
- Necessary to self-consistently include binary inspiral from GW loss rate;
  - We know that significant mass can follow binary through much of this period (Noble++2012);
- Cooling required to regulate vertical thickness;
- Cooling provides a way to include more realistic thermodynamics consistent with its luminosity predictions;
  - No longer have to rely on  $L \sim \dot{M}$  ;
- Eventually radiation feedback important in regions of non-smooth optical depths (e.g., "gap")

# Strategy

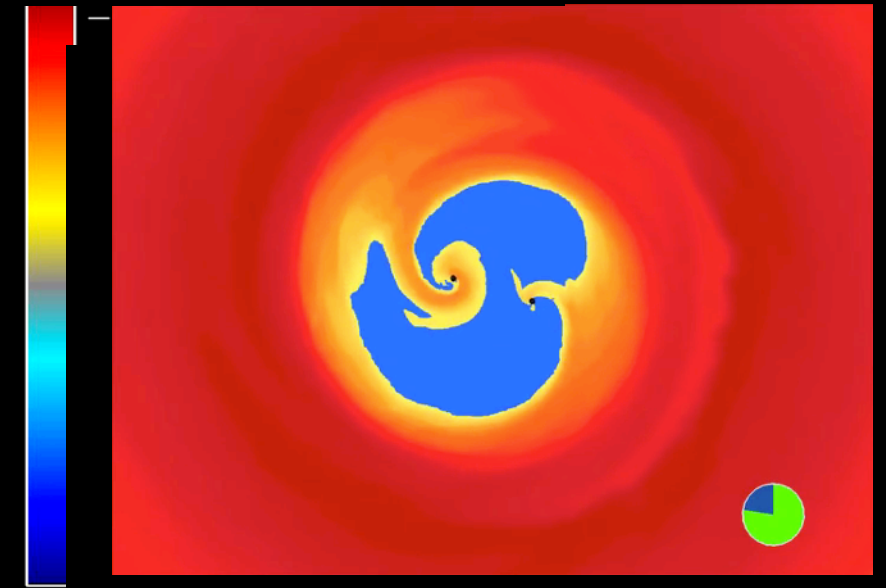
T = 150 Myr

Gas

Hopkins, Hernquist, Di Matteo, Springel++



Noble++2012



Farris++2011

Physical Time (not to scale)

Galactic Merger

Binary Formation

Inspiral

Merger

Re-equilibration

Newtonian Gravity

Numerical Relativity

Post-Newtonian

Static GR

Harm3d

Harm3d

Eulerian, high-resolution/shock-capturing, 3-d, ideal MHD, dynamical GR, HLL fluxes, parabolic reconstruction, dynamical FMR

DATA

DATA



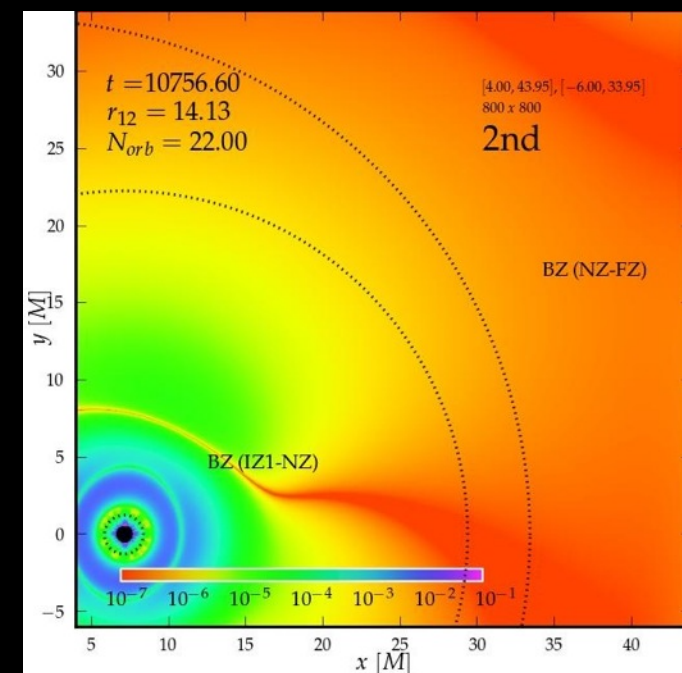
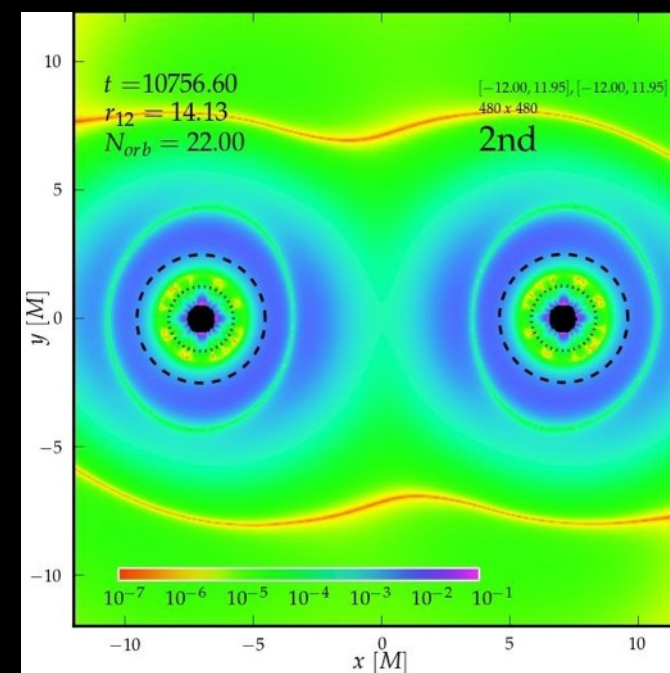
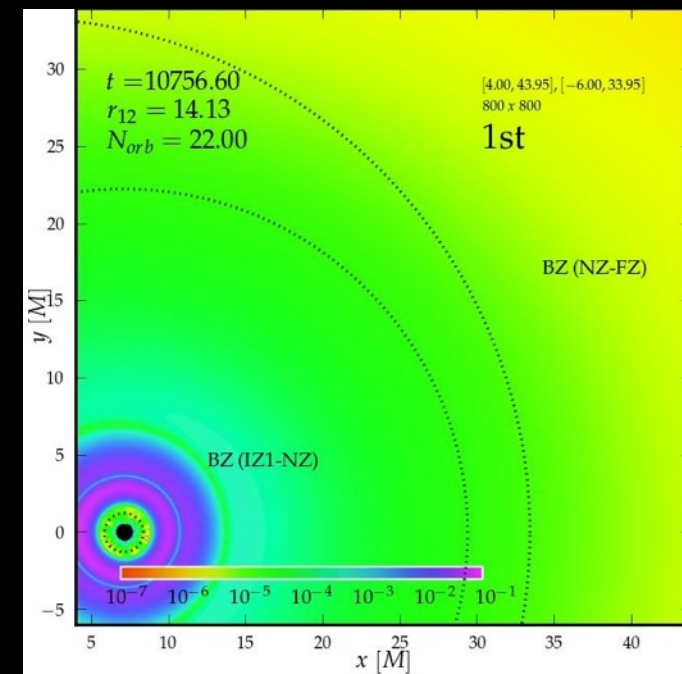
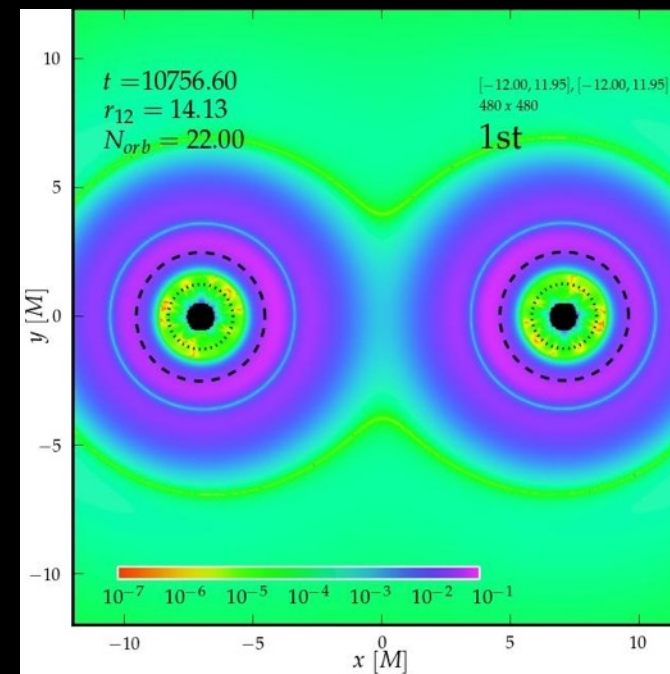
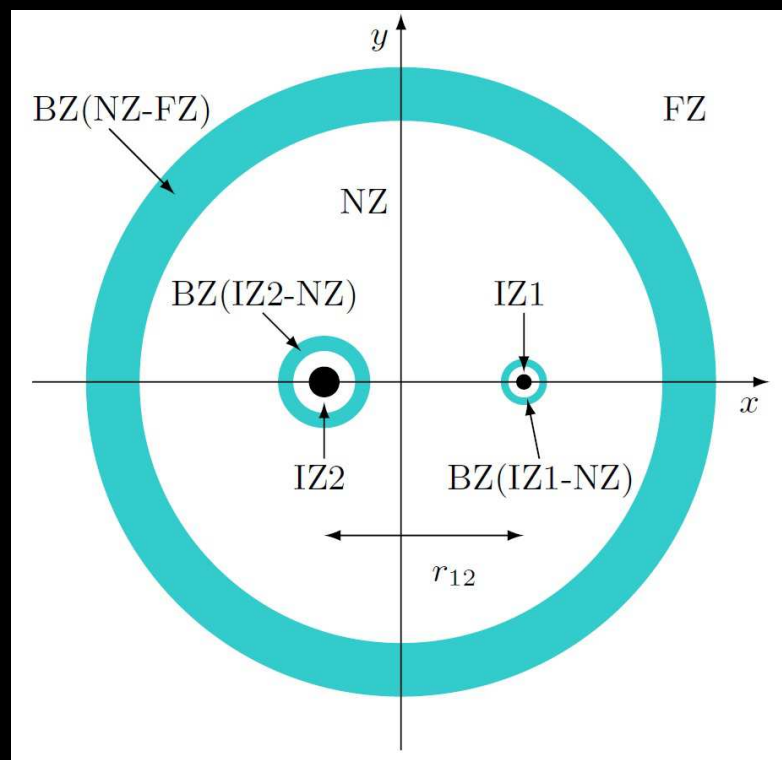
# Approximate Two Black Hole Spacetimes

Yunes++2006, Noble++2012, Mundim++2014

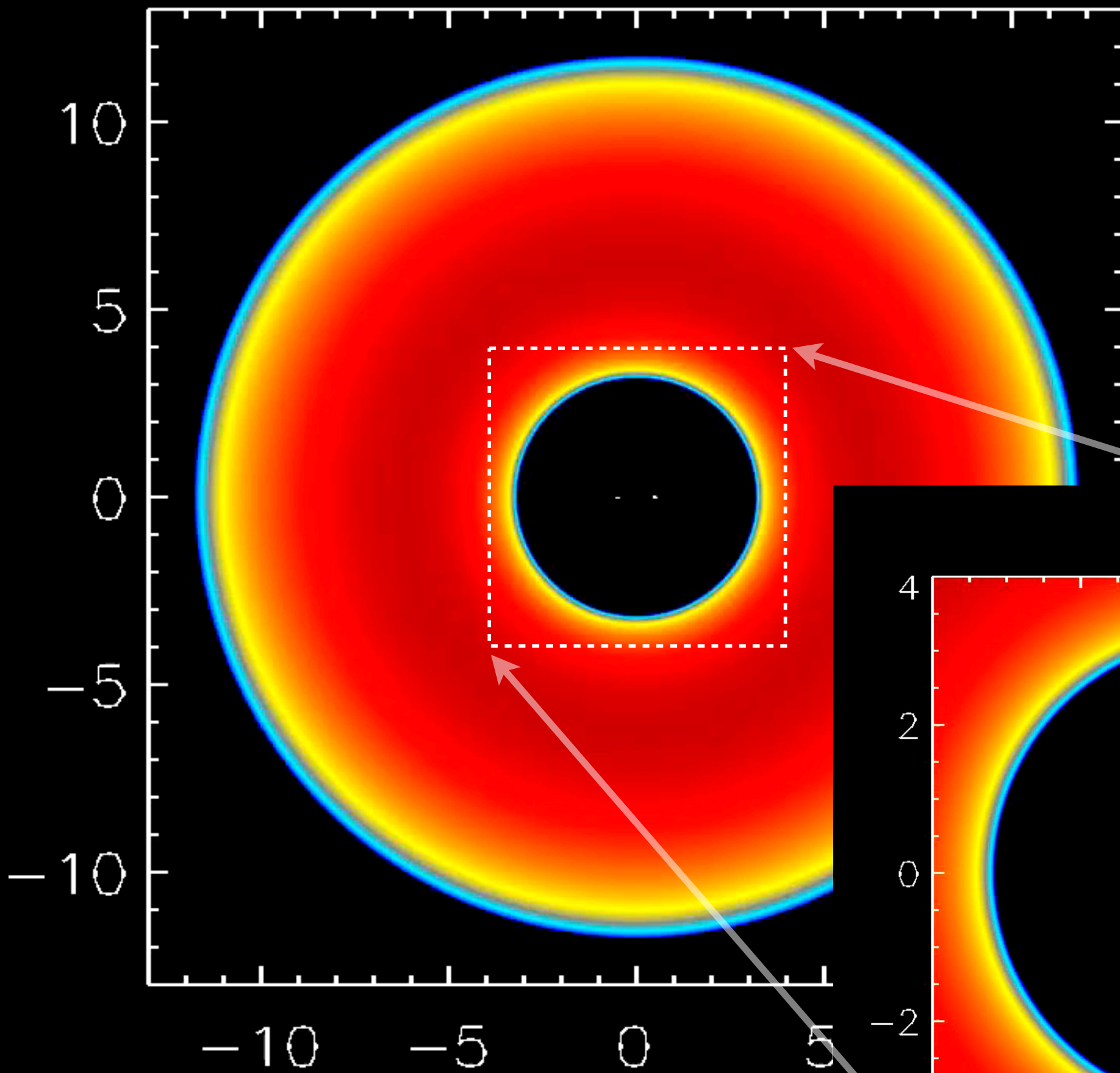
- Solve Einstein's Equations approximately, perturbatively to orders of 2.5 Post-Newtonian order;
- Used as initial data of Numerical Relativity simulations;
- Black hole orbits include radiation-reaction terms;
- BH event horizons are included!
- Closed-form expressions allow us to discretize the spatial domain best for accurate matter solutions and is much simpler to implement;

$$\epsilon_i = m_i/r_i \sim (v_i/c)^2$$

**Ricci Scalar  $\rightarrow 0$**

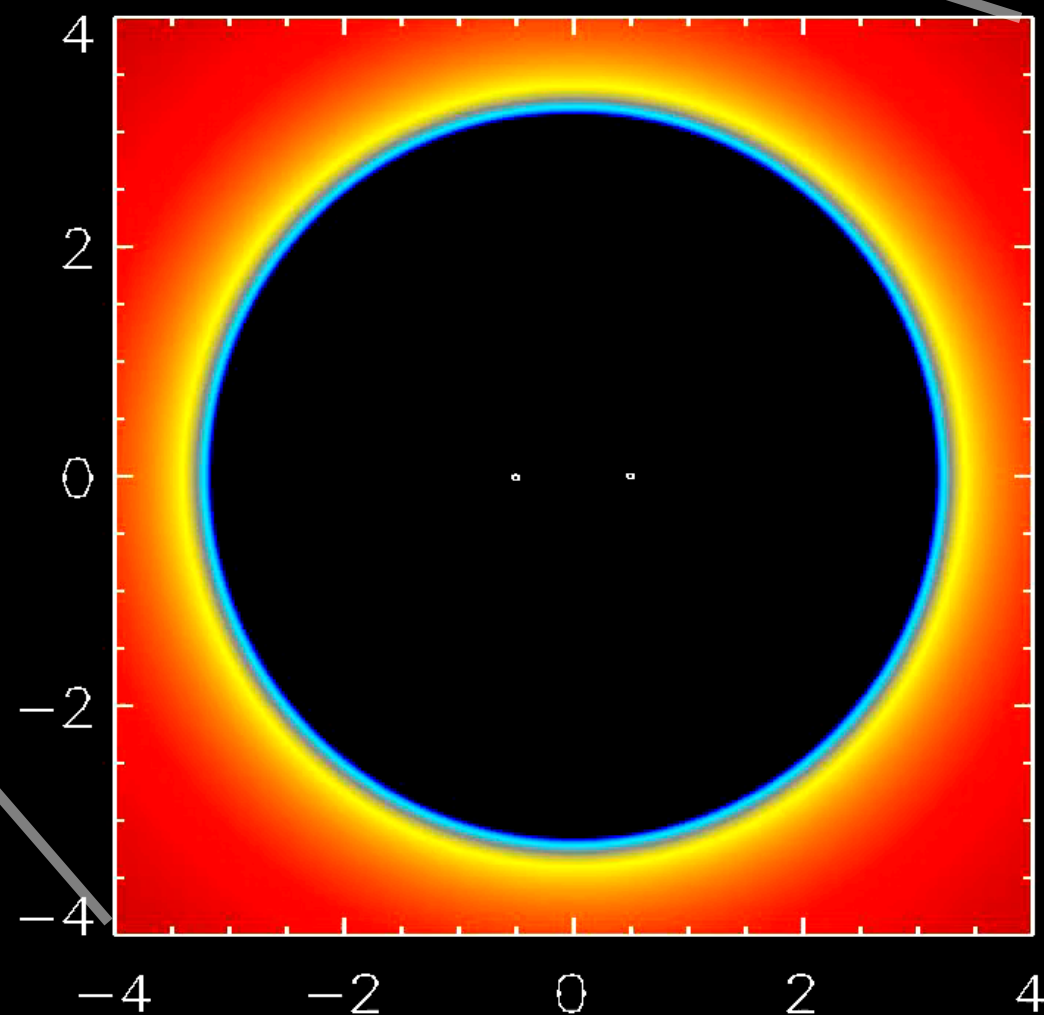


$t = 0.$



- “Excise” BBH to afford  $O(100)$  orbits;
- Simulation bank will be critical to initialize future inspiral studies w/ resolved BH’s;
- Disk starts in “equilibrium”, threaded by poloidal magnetic field;

$t = 0.$

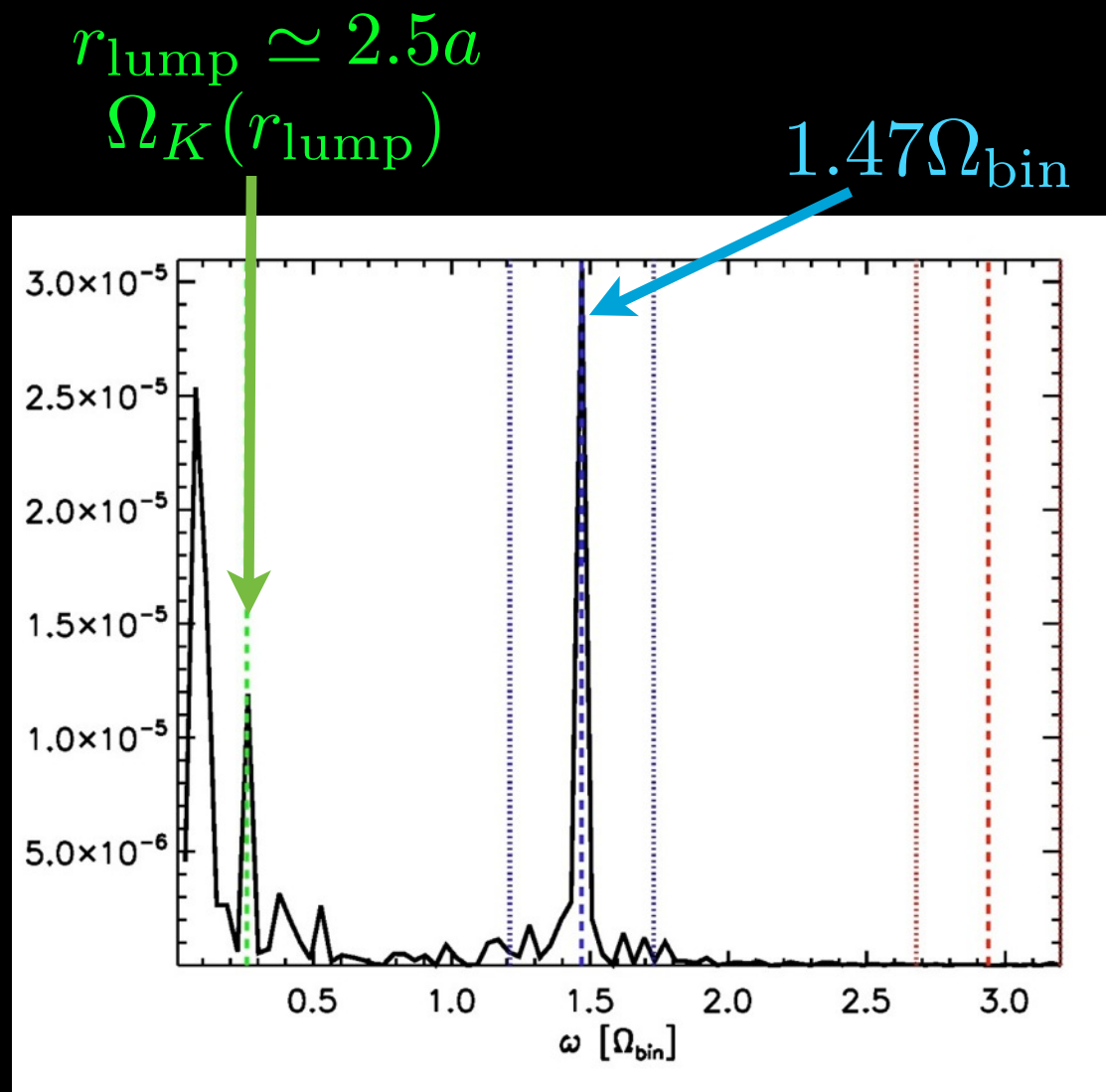




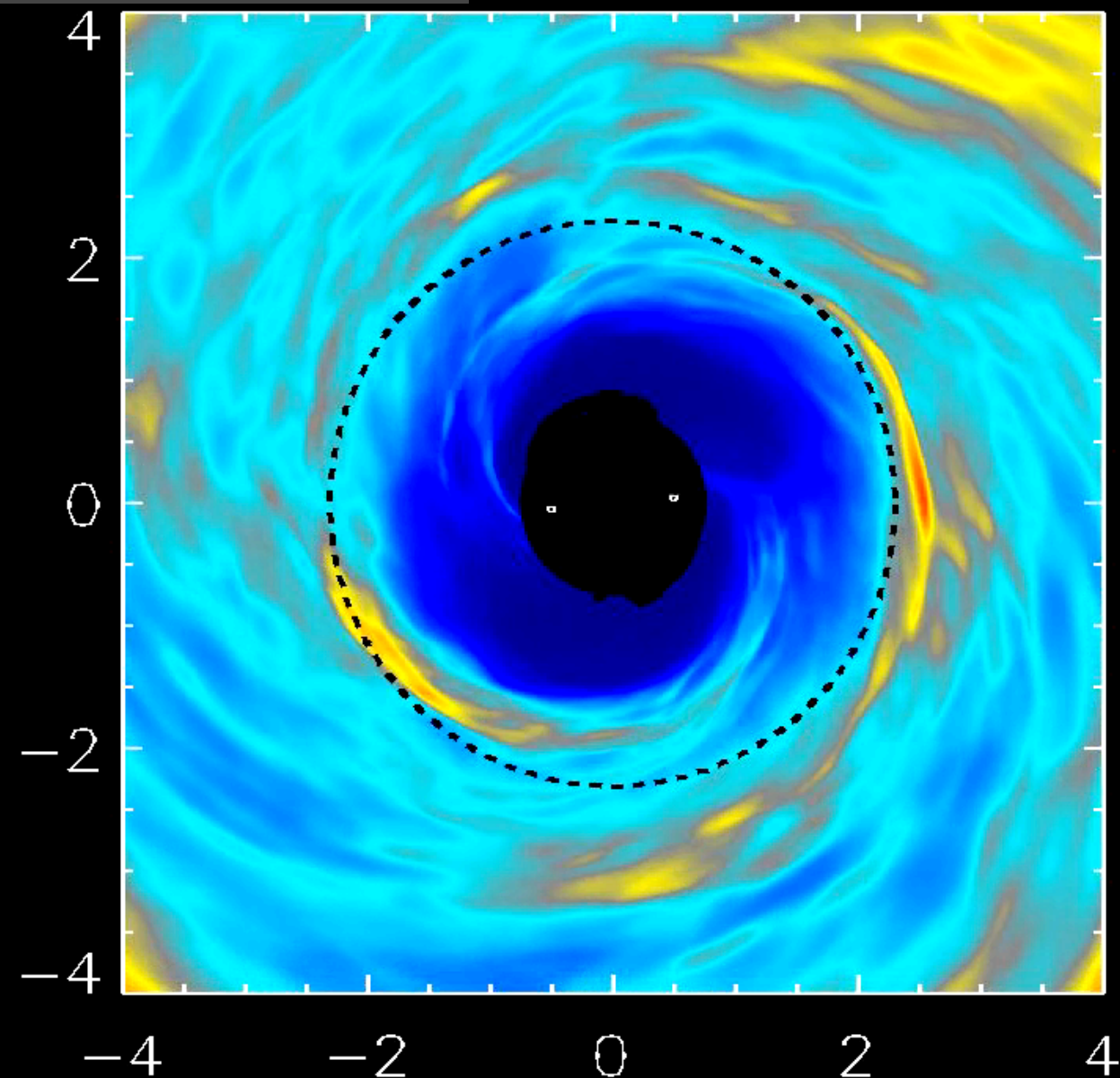
# MHD Simulations with Unresolved BHs:

Noble++2012

## Periodic Signal



**Surface Density**  $t=34950$ .



$$\omega_{\text{peak}} = 2(\Omega_{\text{bin}} - \Omega_{\text{lump}})$$

# Accuracy of Gravity Model

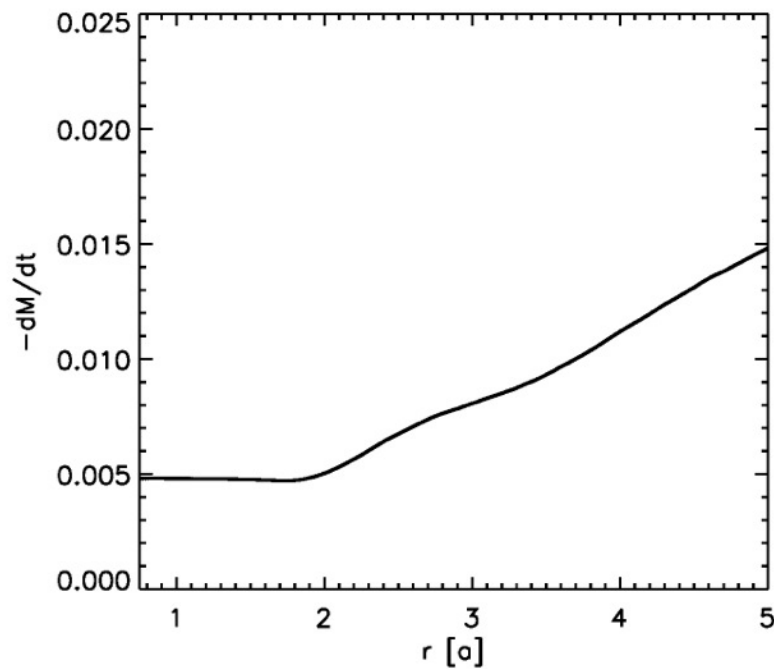
Zilhao++2015

- Turn off highest order PN terms in metric and use the “same” matter initial data;
- Initial Data = Pressure+Rotation Equilibrium;
  - $\longrightarrow \text{Disk} = \text{Disk}(g_{ab})$
  - $\longrightarrow \text{Disk}(g_{ab}[2\text{PN}]) \neq \text{Disk}(g_{ab}[1\text{PN}])$
- Use two strategies for 1PN disk:
  - Disk1: Use *same* orbital parameters as 2PN disk, though it has *different*  $H/R$ ;
  - Disk2: Use *different* orbital parameters as 2PN disk, so that disk has *same*  $H/R$ ;

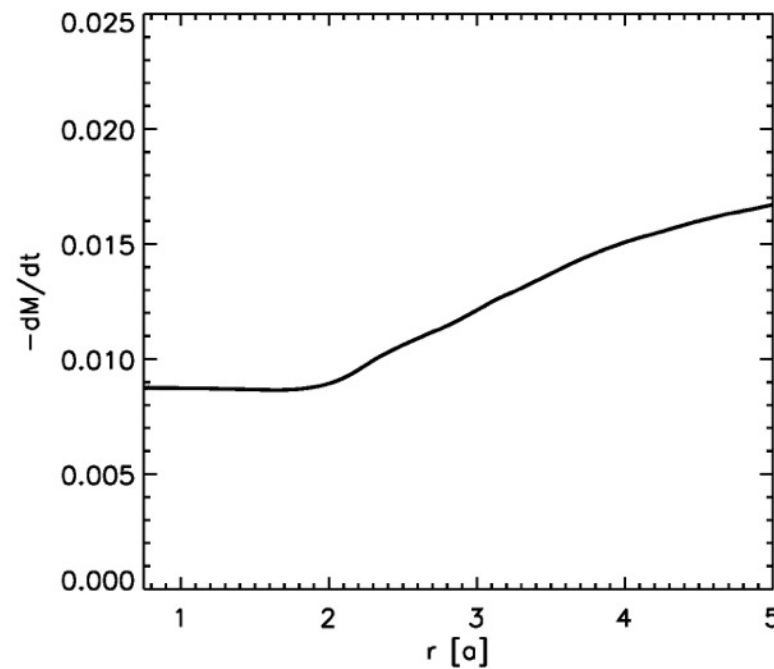


# Variability vs. Post-Newtonian Accuracy:

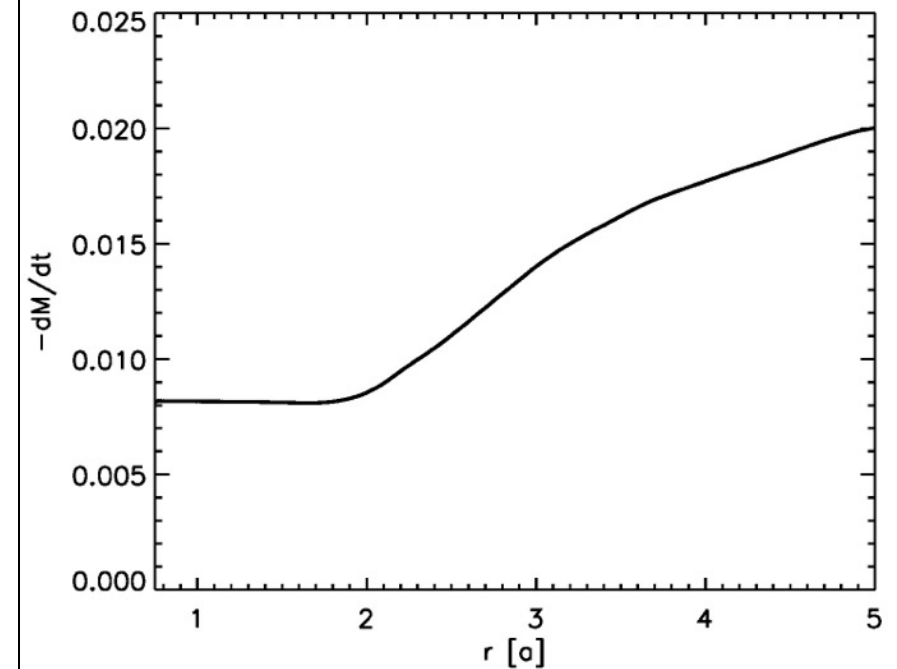
1.5PN  
(Disk1)



1.5PN  
(Disk2)



2.5PN  
(Original)



## Less accurate metrics result in:

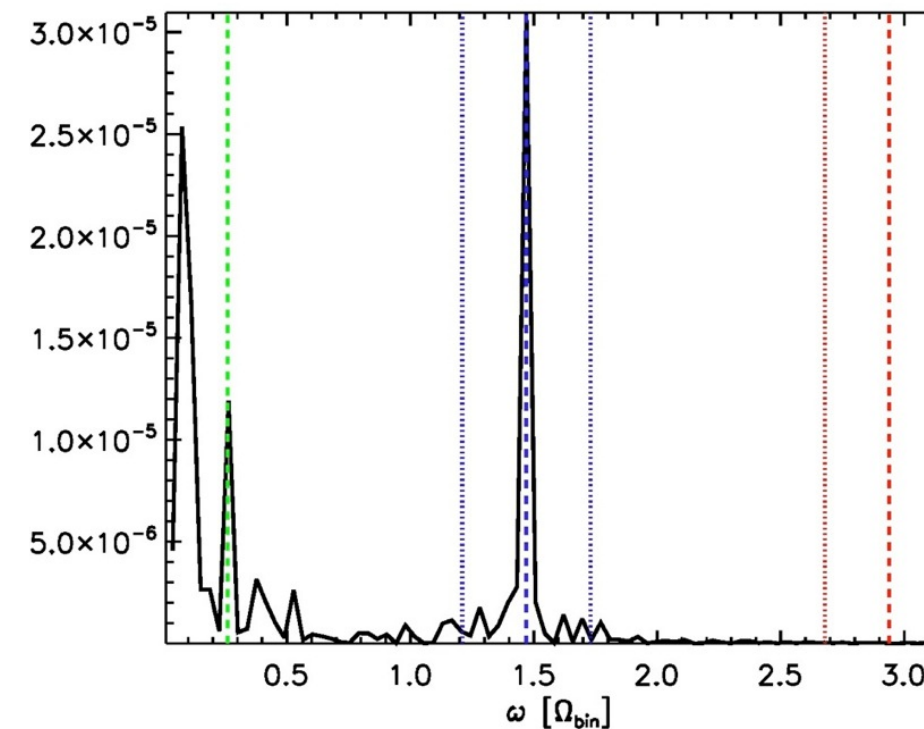
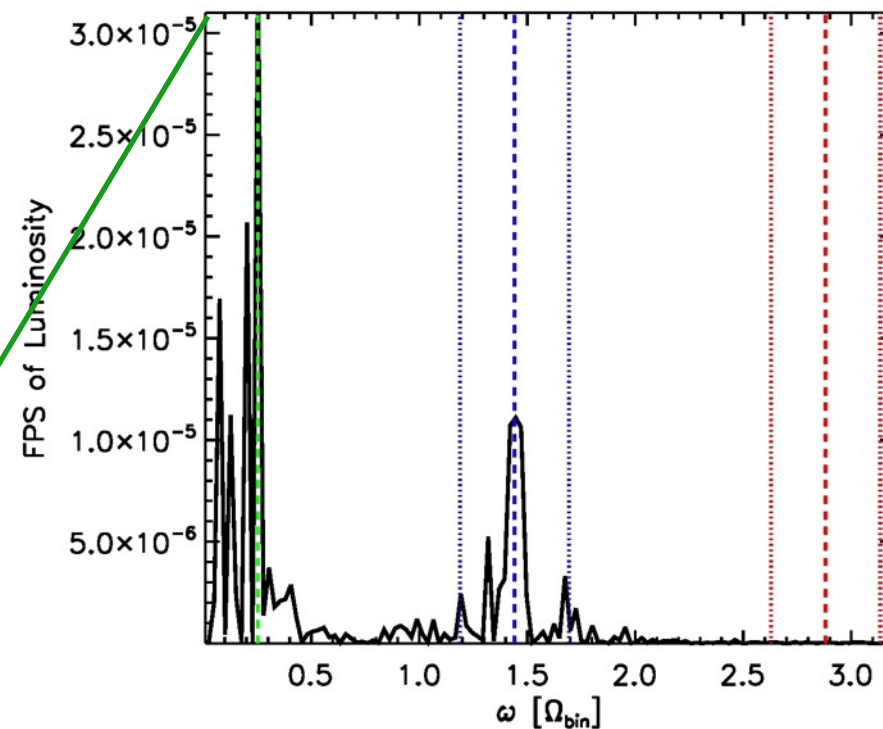
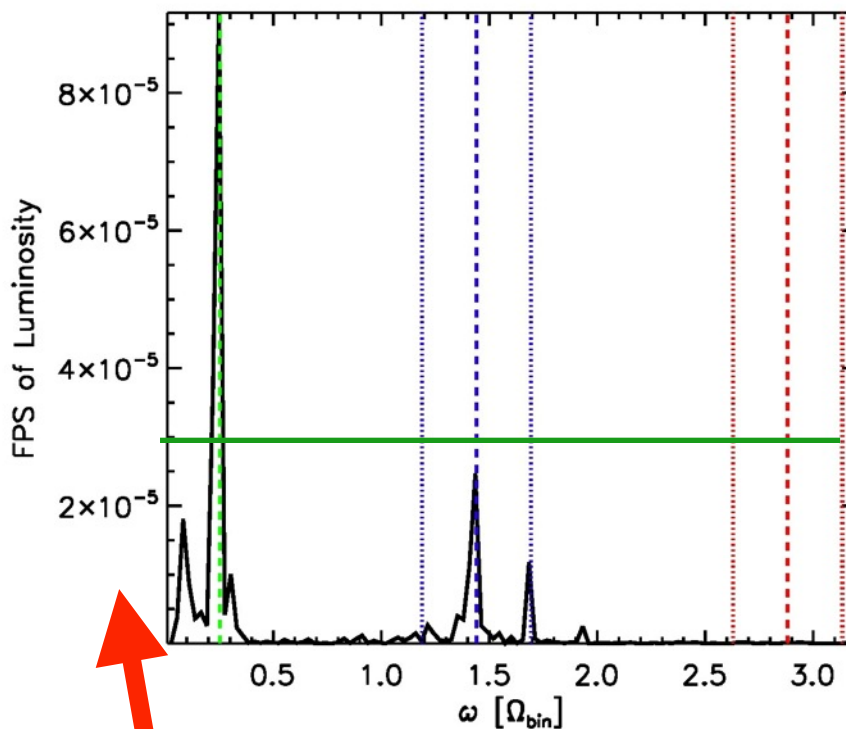
- Fraction of accretion rate through “gap” is approximately the same;
- All other runs we have done also show significant “leakage” rates;

# Variability vs. Post-Newtonian Accuracy:

1.5PN  
(Disk1)

1.5PN  
(Disk2)

2.5PN  
(Original)



Apologies for mismatched scales!

## Less accurate metrics result in:

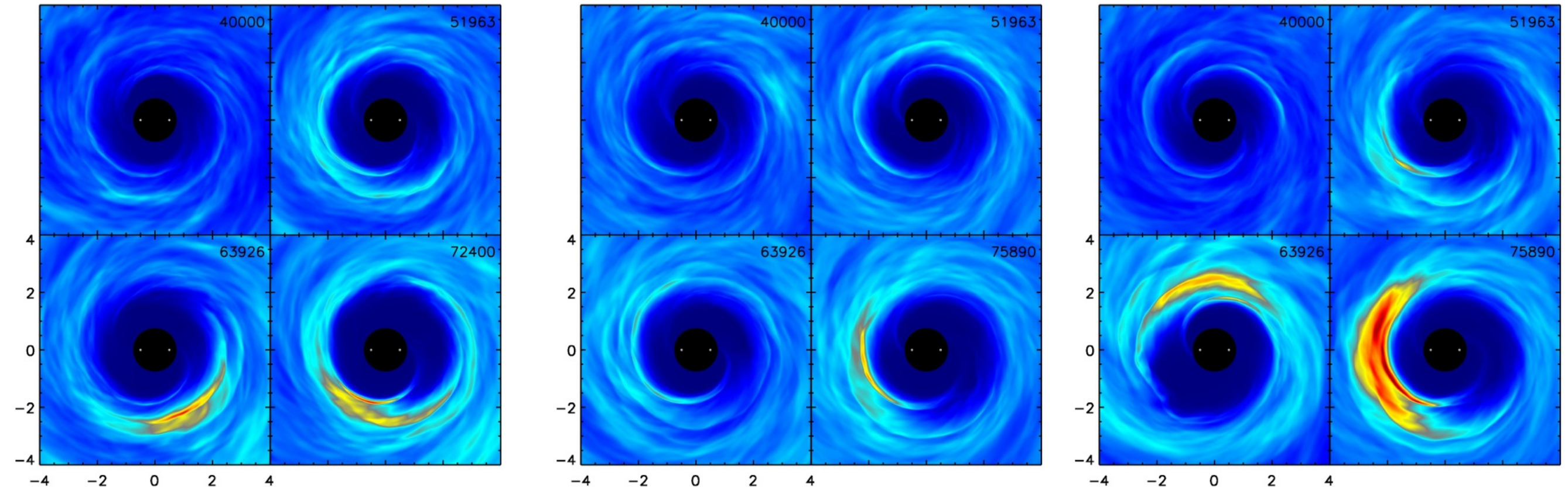
- Stronger variability at lump's orbital frequency;
- Power at beat frequency spread to larger range of frequencies;
- More complex lump/binary modulation;

# Variability vs. Post-Newtonian Accuracy:

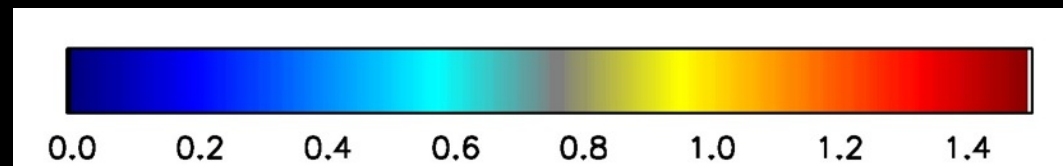
1.5PN  
(Disk1)

1.5PN  
(Disk2)

2.5PN  
(Original)



**Top-down view of Surface Density**



Less accurate metrics result in:

- Slightly weaker  $m=1$  mode or over-density feature;
- Likely explains the increased power at the binary's orbital frequency;

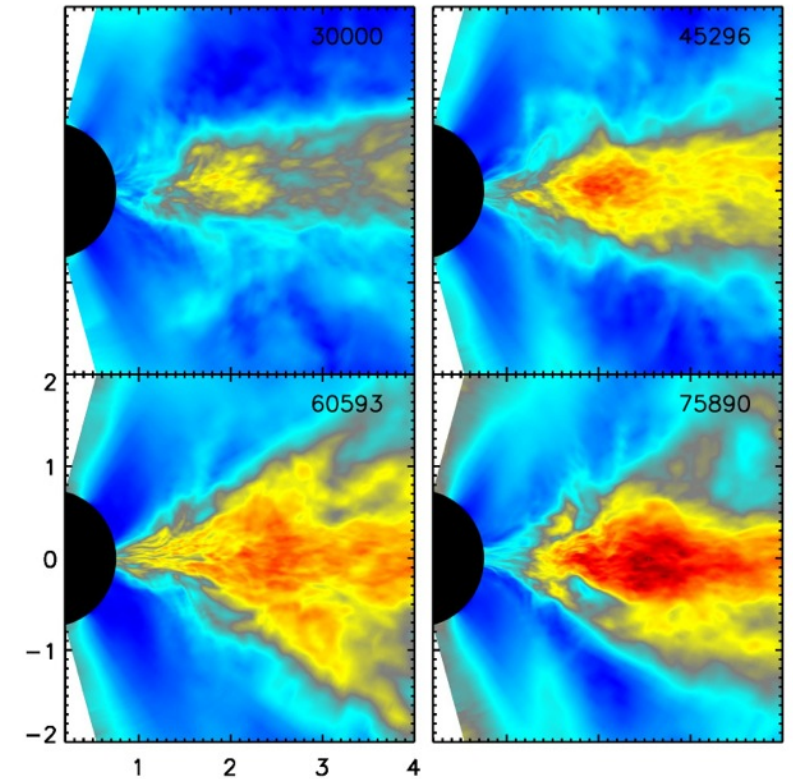
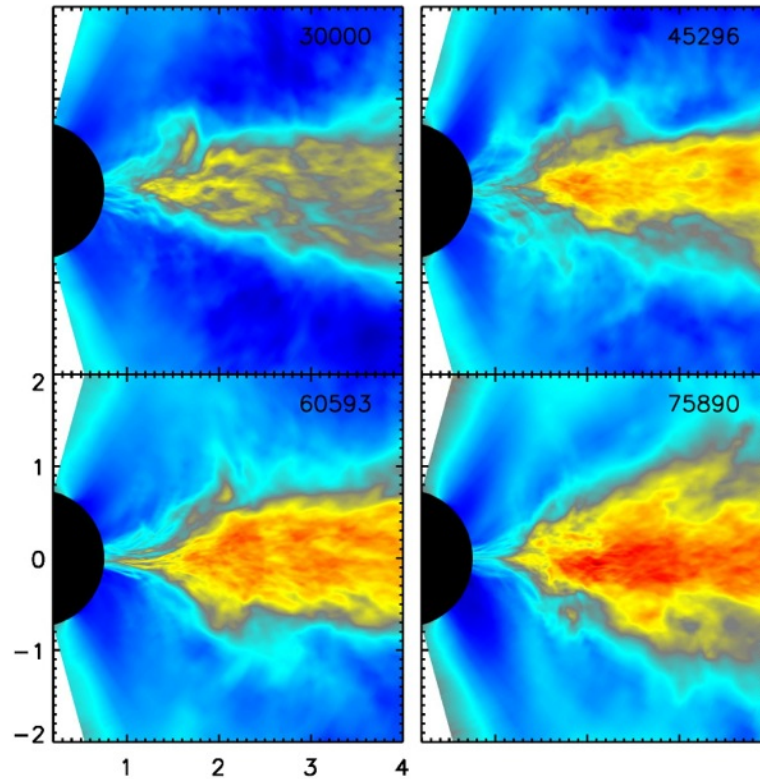
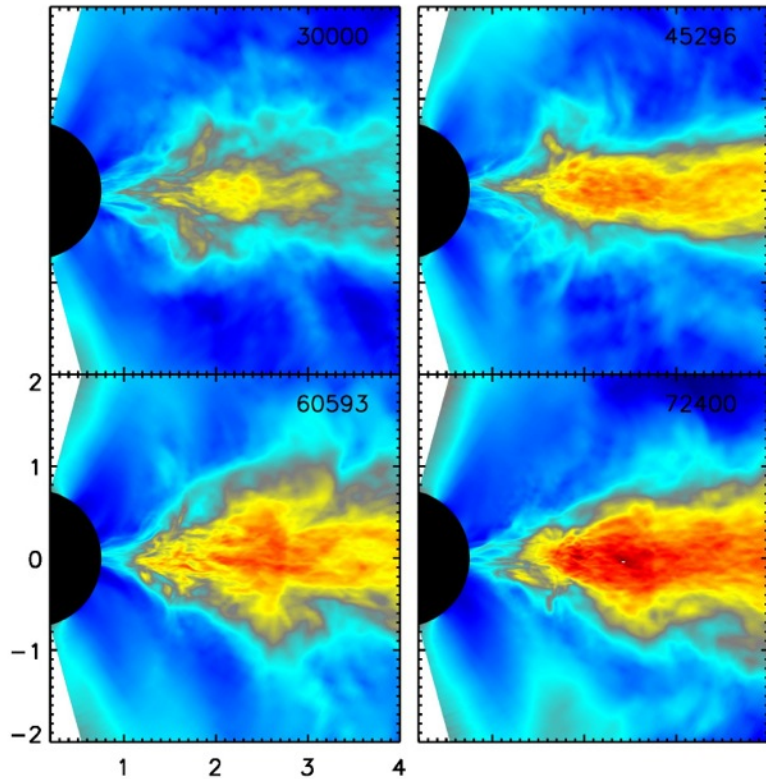


# Variability vs. Post-Newtonian Accuracy:

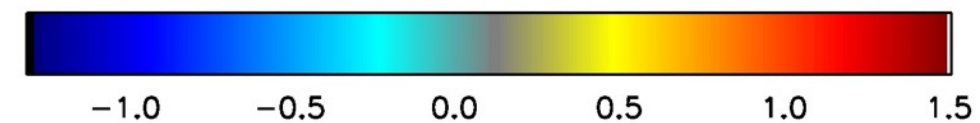
1.5PN  
(Disk1)

1.5PN  
(Disk2)

2.5PN  
(Original)



**Side view of  $\beta = P_{\text{gas}} / P_{\text{mag}}$**



Less accurate metrics result in:

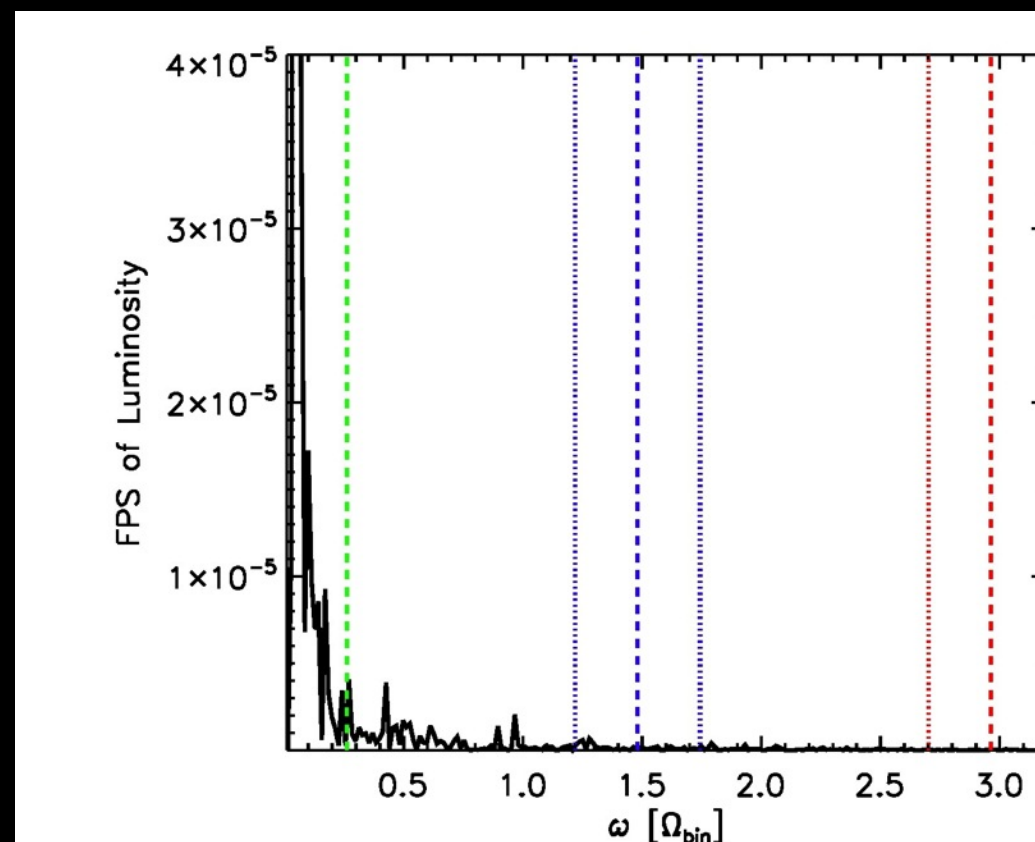
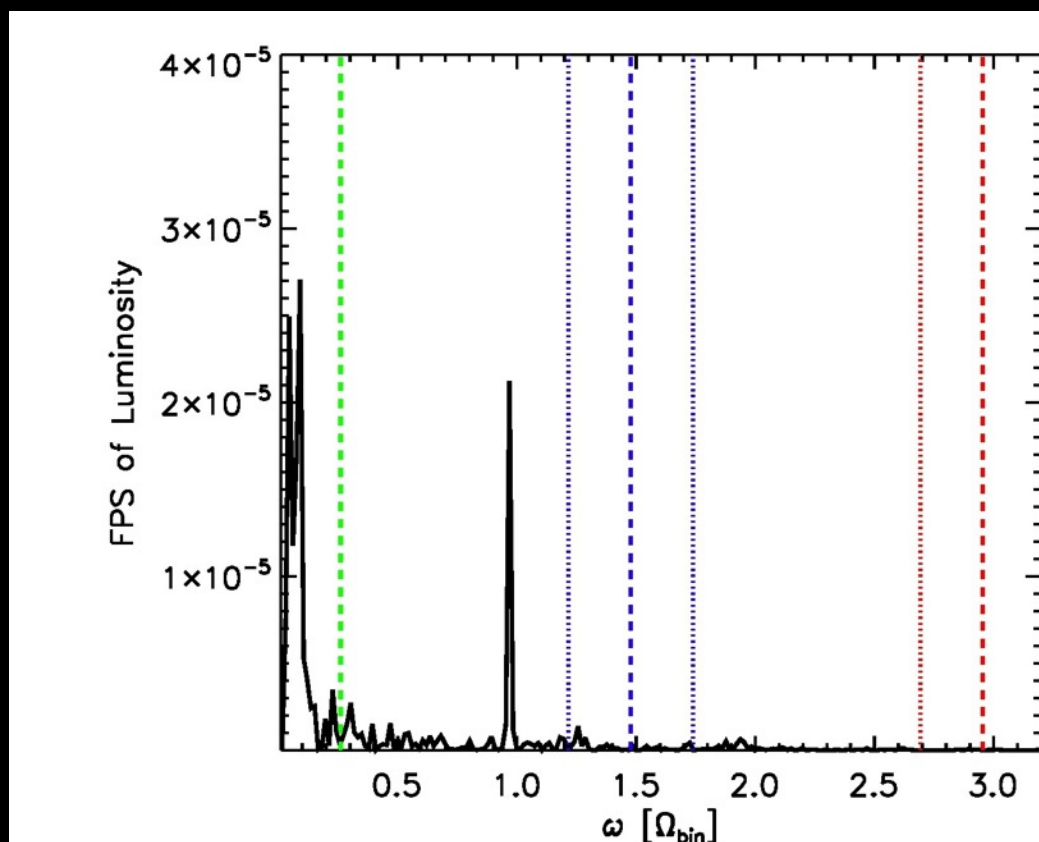
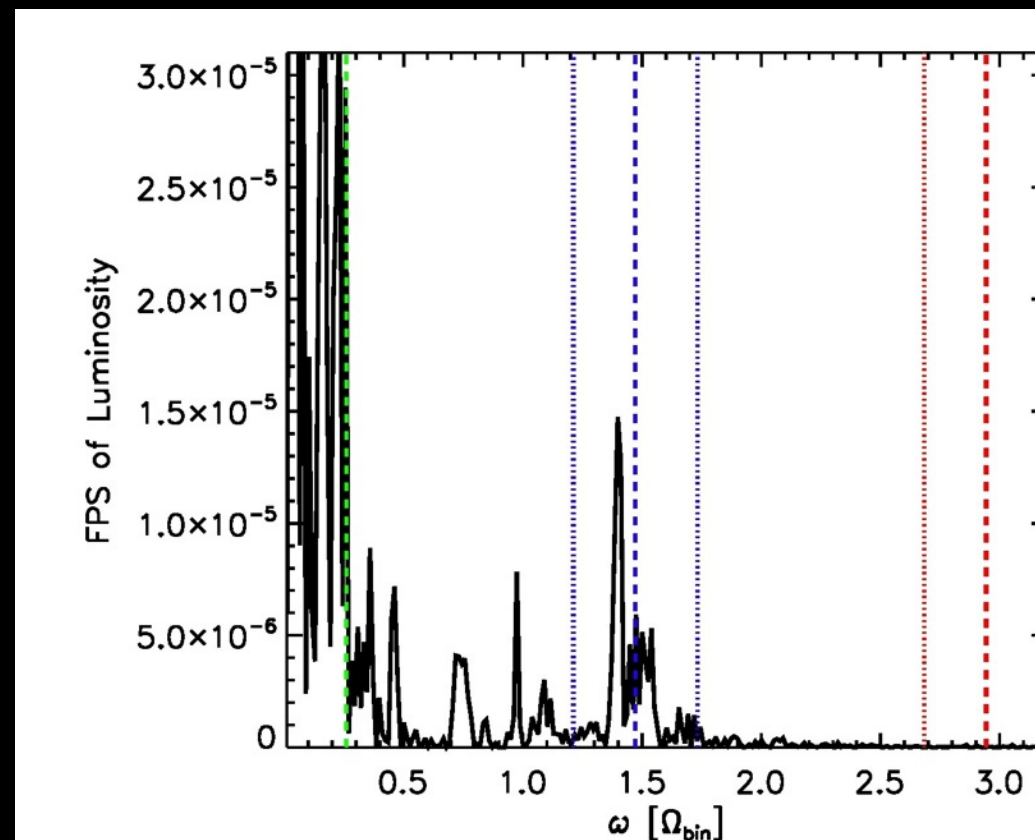
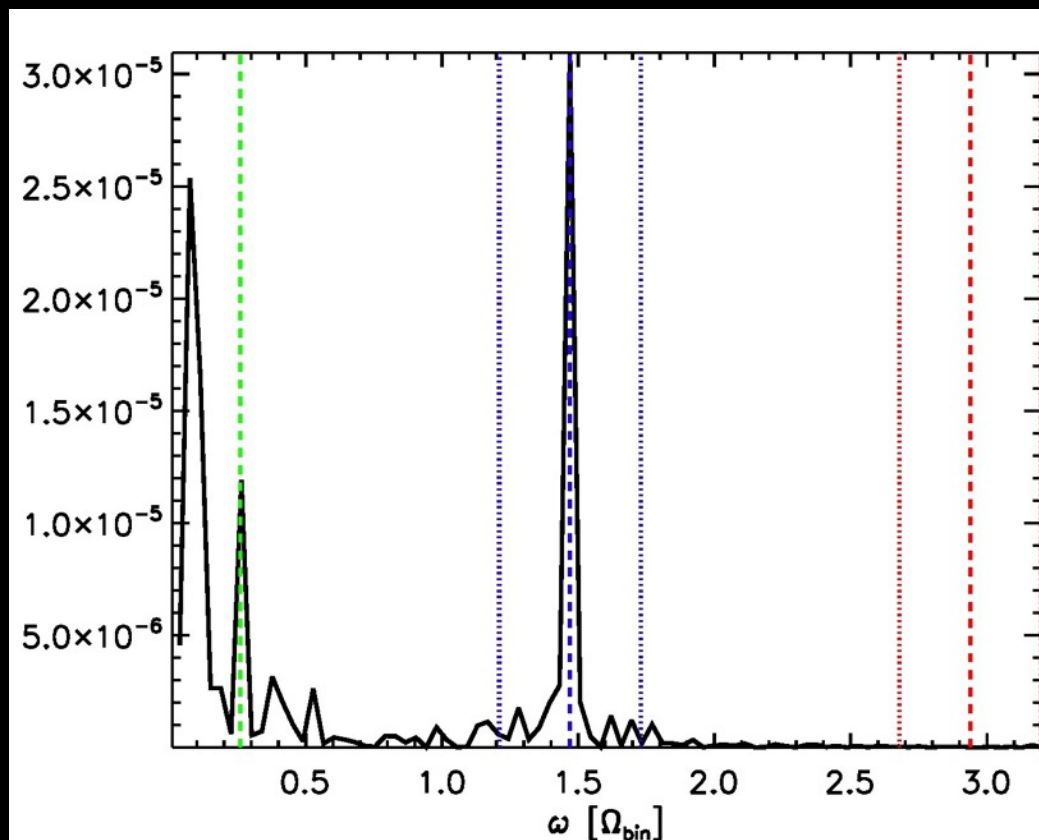
- Slightly less loss of magnetization;
- Possibly due to weaker torque, less dissipation of field from flung out material;
  - Weak torques from “weaker” quadrupole potential;
- Note thicker disk leads to less loss of magnetization;

Zilhao++2015

# Mass Ratio Noble++in-prep

$q=1$

$q=2$



$q=5$

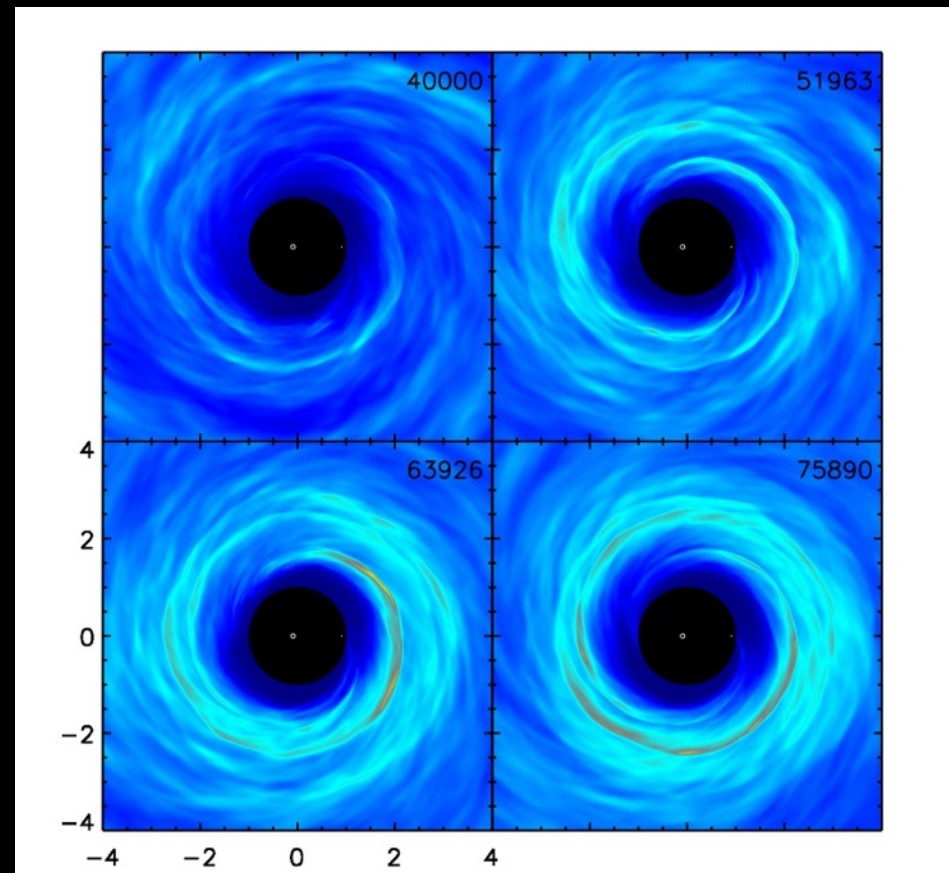
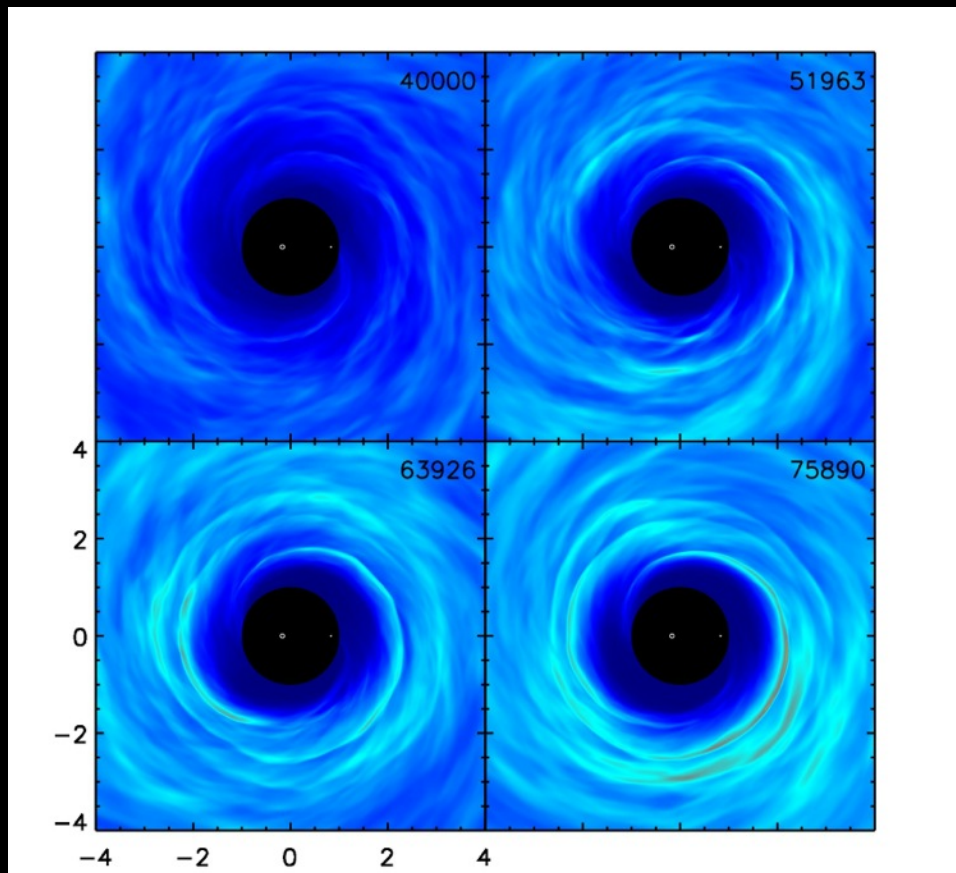
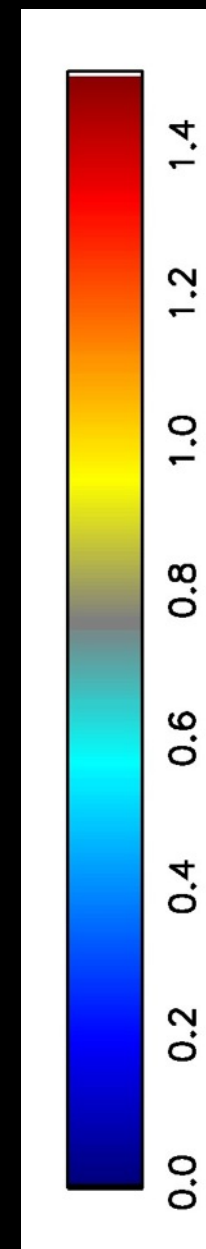
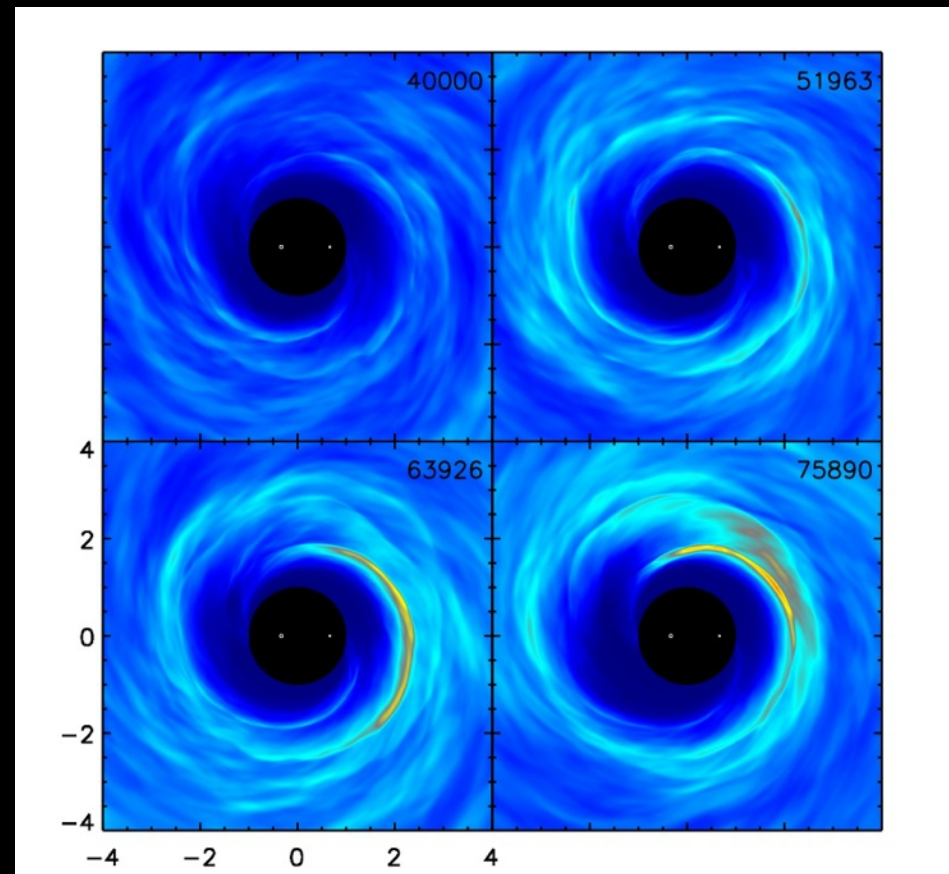
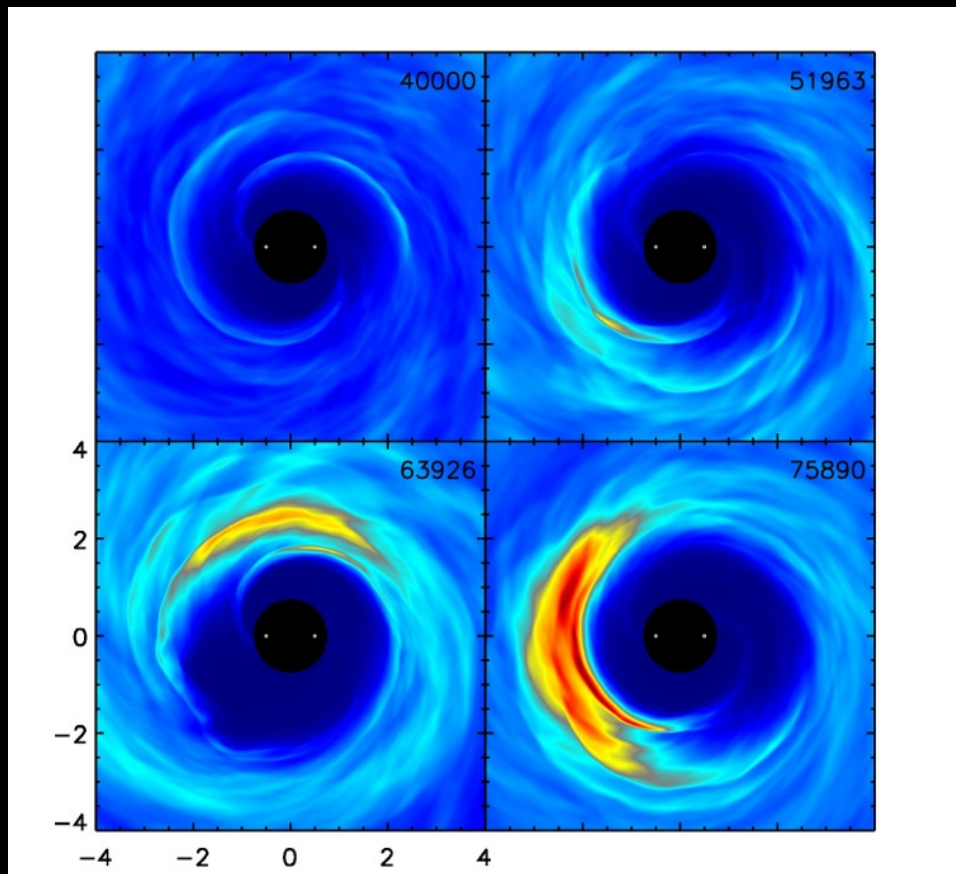
$q=10$



$q=1$

# Mass Ratio Noble++in-prep

$q=2$



$q=5$

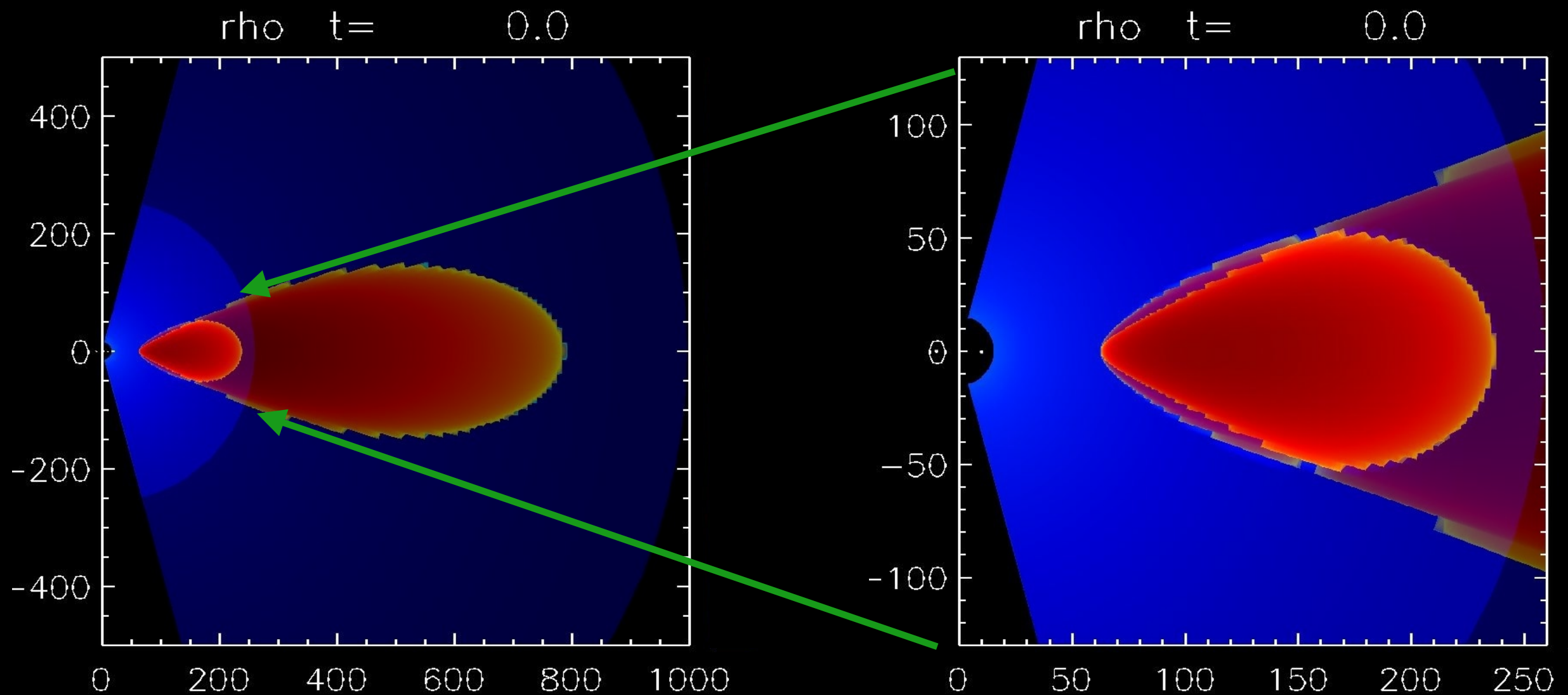
Top-down view of Surface Density

$q=10$



# Disk's State

Noble++in-prep

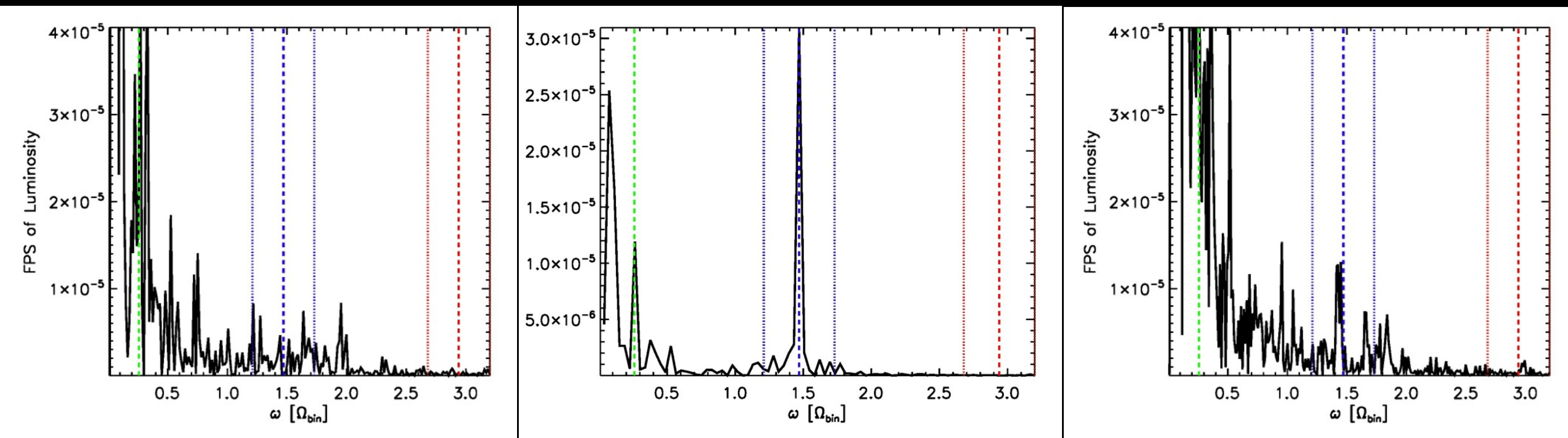


- Bigger disk:
  - “Center” moved from 5a to ~6a;
  - Large extent increases reservoir of magnetic flux and mass;
- Injected flux:
  - Magnetic flux from  $t=0$  added late-time snapshot of original run;
  - Increases local magnetic energy density by only a few percent;

## Bigger Disk

## Original

## Flux-Injected



Again, please note different scales

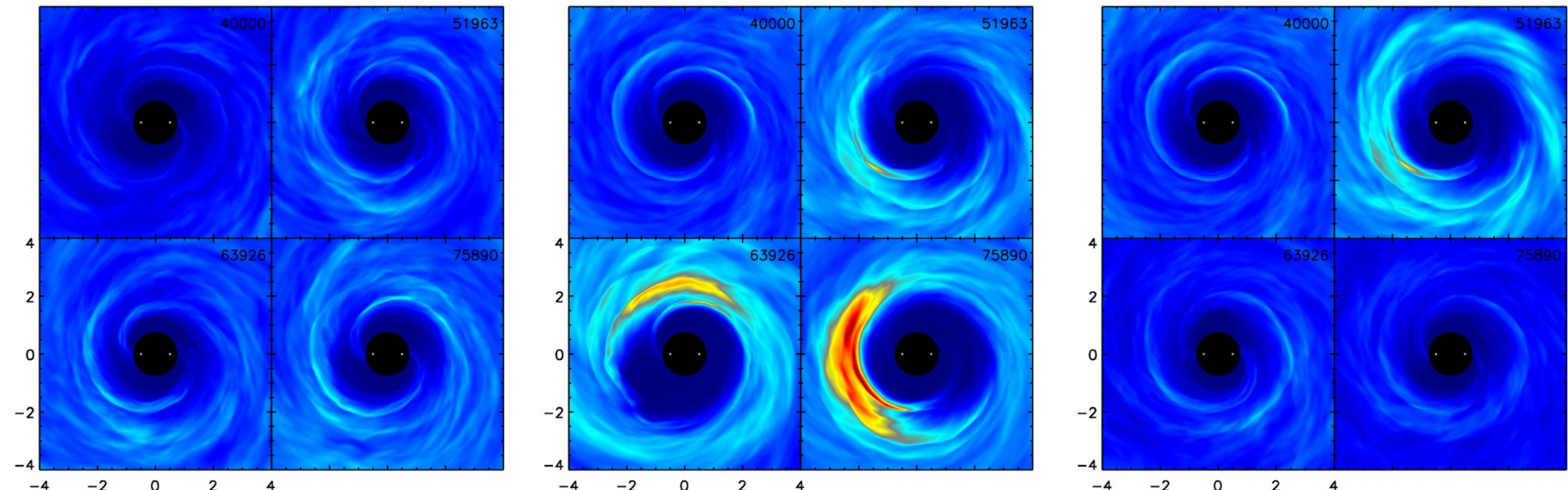
### More magnetic flux led to:

- Less coherent temporal power spectrum;
- Spectra resembling more a slightly bent power law;
- Spectra resembling more spectra from simulations of single black hole disks;
- Is there no over-density?

## Bigger Disk

## Original

## Flux-Injected



### Top-down view of Surface Density

More magnetic flux led to:

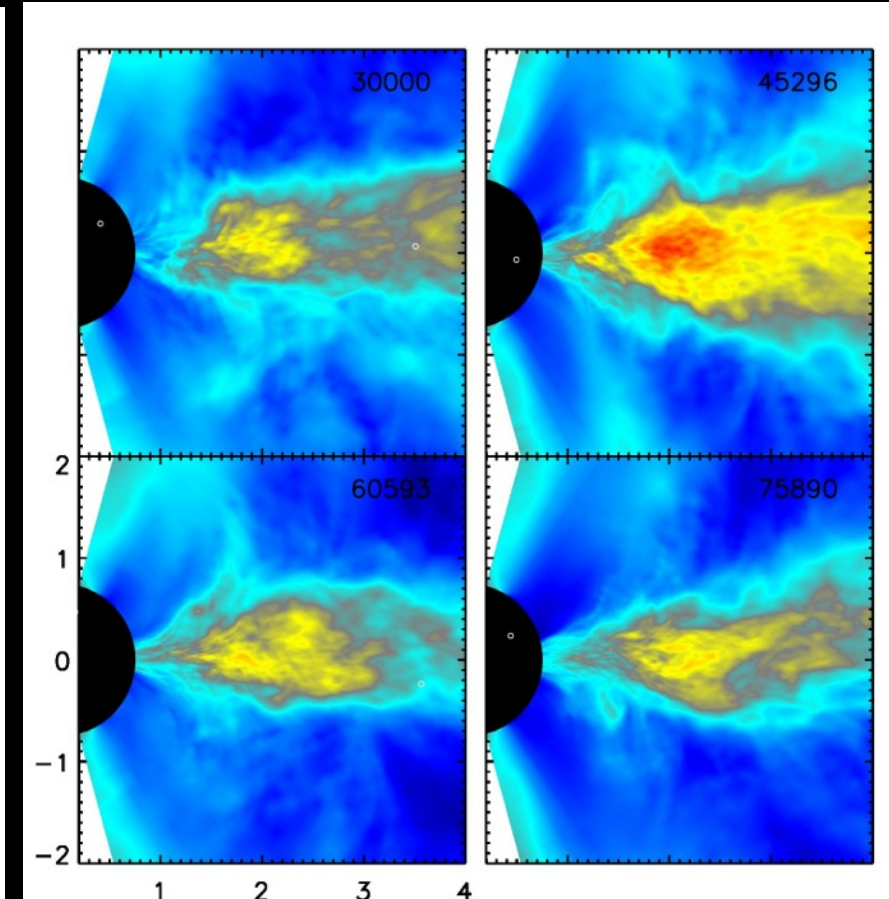
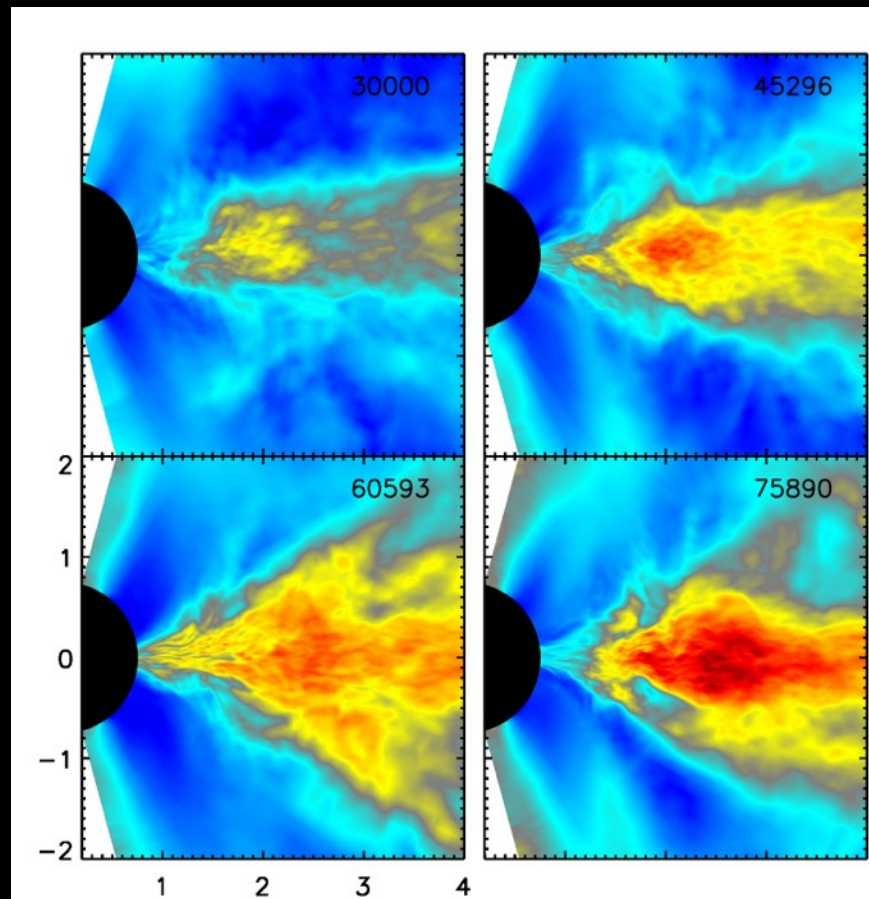
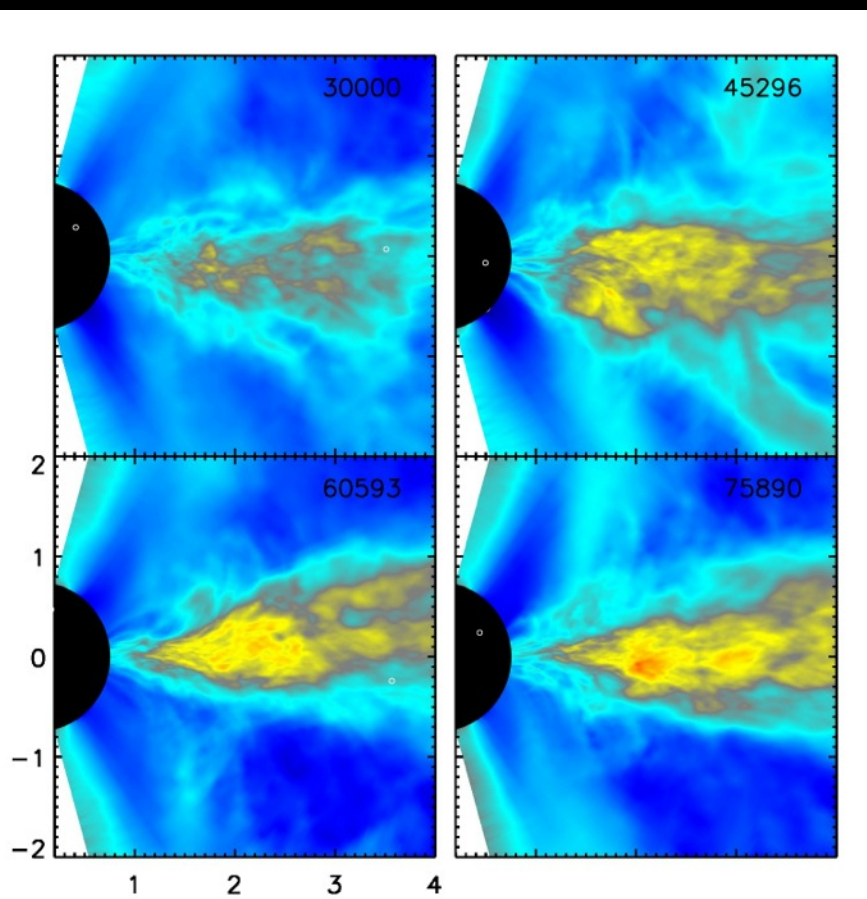
- Much weaker  $m=1$  mode, if any.
- Therefore, no means of developing coherent beat;
- Fluctuations arise just from turbulence;



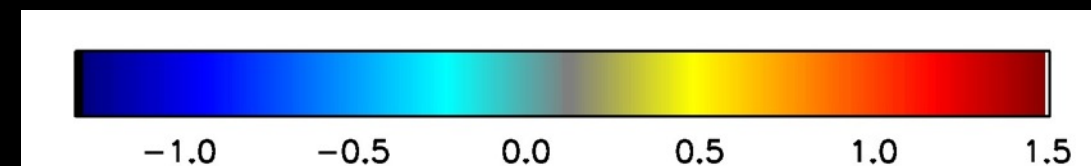
## Bigger Disk

## Original

## Flux-Injected



Side view of  $\text{Beta} = P_{\text{gas}} / P_{\text{mag}}$



- Injected flux led to sustained magnetization throughout over-density region;
- Larger reservoir of flux and mass seems to hinder development of the lump;

# Summary & Conclusions

- Our 3-d MHD simulations in the PN-regime develop a high-Q signal that is non-trivially connected to the binary's orbit;
- We have unexpectedly seen how MHD dynamics can affect the quality of this signal and quash the development of the overdensity;
- At a separation of  $20M$ , with equal-mass binaries, differences in the metric at 1.5PN and 2.5PN orders are insignificant compared to stochastic error;
- The PN-accuracy effects will likely be even smaller for smaller mass ratios;
- Overdensity and the “beat signal” disappear somewhere  $2 < q < 5$ ;
- No coherent signal of any kind seen at  $q=10$ ;